## U.S. DEPARTMENT OF COMMERCE NATIONAL BUREAU OF STANDARDS Washington, D.C. 20234

LETTER CIRCULAR LC 1035

# UNITS AND SYSTEMS OF WEIGHTS AND MEASURES $\frac{1}{}$ THEIR ORIGIN, DEVELOPMENT, AND PRESENT STATUS

## 1. Introduction

The National Bureau of Standards was established by act of Congress in 1901 to serve as a National scientific laboratory in the physical sciences and to provide fundamental measurement standards for science and industry. In carrying out these related functions the Bureau conducts research and development in many fields of physics, mathematics, chemistry, and engineering. At the time of its founding, the Bureau had custody of two primary standards the meter bar for length and the kilogram cylinder for mass (or weight). With the phenomenal growth of science and technology over the past half century, the Bureau has become a major research institution concerned not only with everyday weights and measures but also with hundreds of other scientific and engineering standards that have become necessary to the industrial progress of the Nation. Nevertheless, the country still looks to the Bureau for information on the units of weights and measures, particularly their definitions and equivalents.

The subject of weights and measures can be treated from several different standpoints. Scientists and engineers are interested in the methods by which precision measurements are made; State weights and measures officials are interested in laws and regulations on the subject and in methods of verifying commercial weighing and measuring devices. But a vastly larger group of people are interested in some general knowledge of the origin and development of weights and measures, of the present status of units and standards, and of miscellaneous facts that will be useful in everyday life. This Letter Circular has been prepared to supply that information on weights and measures that experience has shown to be the common subject of inquiry.

#### 2. Units and Systems of Weights and Measures

The expression "weights and measures" is used in this Letter Circular in its basic sense of referring to measurements such as length, mass, and capacity, thus excluding such topics as electrical measurements and thermometry. This section on units and systems of weights and measures presents some fundamental information to clarify thinking on this subject and to eliminate erroneous and misleading use of terms.

<sup>1/</sup> This Letter Circular is being issued as a temporary replacement of Circular 570 (issued May 1956), which is now out of print and is being revised. SEE PAGE 32 FOR REDEFINITION OF THE METER AND INFORMATION ON NEW STANDARDS OF LENGTH, MASS, AND TIME.

## 2.1. Origin and Early History of Units and Standards

#### a. Units and Standards

It is essential that there be established and kept in mind the distinction between the terms "units" and "standards."

A unit is a value, quantity, or magnitude in terms of which other values, quantities, or magnitudes are expressed. In general, a unit is fixed by definition and is independent of such physical conditions as temperature. Examples: The yard, the pound, the gallon, the meter, the liter, the gram.

A standard is a physical embodiment of a unit. In general it is not independent of physical conditions, and it is a true embodiment of the unit only under specified conditions. For example, a yard standard has a length of one yard when at some definite temperature and supported in a certain manner. If supported in a different manner, it might have to be at a different temperature in order to have a length of 1 yard.

## b. General Survey of Early History of Weights and Measures

The beginnings of the development of weights and measures go back to primitive man in prehistoric times. Hence, there is a great deal of uncertainty about the origin and early history of weights and measures. Many believe that the units first used by primitive man were those of length and weight and that units of area, volume, and capacity were of much later origin. Units of length may have been the earliest. These were derived from the limbs of the human body, and included the length of the foot, the width of the palm, the length of the forearm, etc. Units of weights included weights of kernels of grain and weights of shells.

At first these units were not very definitely defined. Later they became somewhat more definite when, for example, the foot became the length of the foot of a tribal chief or other ruler. At a much later date physical standards were made and deposited for safekeeping in a temple or other place of security. These early physical standards were usually very crude; it is generally considered, however, that they were as satisfactory for the needs of the people at that time as our most modern standards are for our own needs.

Our present knowledge of early weights and measures comes from many sources. Some rather early standards have been recovered by archeologists and preserved in museums. The comparison of the dimensions of buildings with the descriptions of contemporary writers is another source of information. An interesting example of this is the comparison of the dimensions of the Greek Parthenon with the description given by Plutarch from which a fairly accurate idea of the size of the Attic foot is obtained. In some cases we have only plausible theories and we must sometimes decide on the interpretation to be given to the evidence. For example, does the fact that the length of the double-cubit of early Babylonia was equal (within two parts in a thousand) to the length of the seconds pendulum at Babylon indicate a scientific knowledge of the pendulum at a very early date, or do we merely have a curious coincidence? By studying the evidence given by all available sources, and by correlating the relevant facts, we obtain some idea of the origin and development of the units. We find that they have changed more or less gradually with the passing of time in a complex manner because of a great variety of modifying influences. We find the units modified and grouped into systems of weights and measures: The Babylonian system, the Phileterian system of the Ptolemaic age, the Olympic system of Greece, the Roman system, and the British system, to mention only a few.

#### c. Origin and Development of Some Common Units

The origin and development of units of weights and measures has been investigated in considerable detail and a number of books have been written on the subject. It is only possible to give here somewhat sketchily the story about a few units.

One of the earliest units was the <u>foot</u>. This was first the length of the human foot without further specification or modification, then the length of the foot of various rulers of tribes and groups of people. Later, by gradual evolution, it was the foot as used in succession by the Egyptians, Greeks, and Romans, brought to Britain by the Romans, modified with the passing of time, and finally defined in Great Britain as 1/3 of the British Imperial Yard and in this country as 1/3 of the U. S. yard.

A very interesting and important unit of length used by many ancient peoples was the <u>cubit</u>, originally defined as the distance from the point of the elbow to the end of the middle finger. This unit was about 18 inches long, but there were important variations in the length of a cubit.

The inch was originally a thumb's breadth. In the Roman duodecimal system it was defined as 1/12 foot, and was introduced into Britain during Roman occupation, where it became a part of the English system of weights and measures.

The mile was defined by the Romans as 1 000 paces\* or double steps, the pace being equal to 5 Roman feet. This Roman mile of 5 000 Roman feet was introduced into Britain, became 5 000 English feet, and in Tudor times (probably in the reign of Henry VII, 1485 to 1509, but definitely by a statute of Queen Elizabeth, who reigned 1558 to 1603) was changed to 5 280 feet in order to make the furlong of 1/8 mile equal to the rood of 660 feet, or 220 yards (40 rods of 16 1/2 feet, or 5 1/2 yards each).

The yard as a unit of length is apparently of much later origin than the units previously discussed. It appears to have had a double origin: (1) as the length of an Anglo-Saxon gird or girdle, and (2) as the length of the double

<sup>\*</sup> It should be noted that a space has been inserted instead of commas in all of the numerical values given in this Letter Circular, following a growing practice originating in tabular work to use the space to separate large numbers into groups of three digits.

cubit. There is an old tradition, often stated as a fact, that Henry I decreed that the yard should thenceforth be the distance from the tip of his nose to the end of his thumb.

The point is the basic unit for measuring type. This unit originated with Pierre Simon Fournier in 1737. It was modified and developed by the Didot brothers, Francois Ambroise and Pierre Francois, in 1755. It was first put into effect in the United States by a Chicago type foundry (Marder, Luse, and Company) in 1878. As adopted in 1886 by the American Type Founders' Association and now defined in the United States, Canada, and Great Britain, it is 0.013 837 inch, a value only slightly less than 1/72 inch.

Of units of weight, one of the earliest is the grain, which was originally the weight of a grain of wheat or of some specified seed native to some particular locality.

The Roman pound (libra) was the hundredth part of an older weight, the talent, which is believed to have been originally the weight of an Egyptian royal cubic foot of water. The Roman pound was divided into 12 ounces (unciae, meaning twelfth parts) of 437 grains each. This system was introduced into Britain where the pound was increased so as to have 16 of the original ounces. This pound became known as the avoirdupois pound, the word avoirdupois meaning "goods of weight." The idea of a pound divided into 16 parts was not a new one, as the Greeks had divided their pound into 16 parts, as well as into 12 parts. The pound, which in England had long been used for mint purposes and called the troy pound, consisted of 5 760 grains (12 ounces of 480 grains each). The origin of this troy pound and troy ounce is very uncertain. One theory is that the troy pound came from Troyes, France, but there seems to be a serious question whether even the name had its origin in that place. Sometime prior to 1600 A. D., the avoirdupois pound was increased by 8 grains so that it would consist of 7 000 grains instead of 6 992 grains and thus the number of grains in the avoirfupois pound would have a more simple ratio to the number of grains in the troy pound, which, being used for mint purposes, it was considered advisable to keep unchanged.

That the ton was the weight of a certain volume of some material is highly probable. Among the Anglo-Saxons it may have been the weight of a quantity of wheat in 32 bushels, that is, in 1 chaldron.

The stone was an early unit of weight in the British Isles. At one time it appears to have been 16 pounds in the system: 16 pounds = 1 stone, 16 stones = 1 wey, 16 weys = 1 last, and 1/2 last = 1 ton (not the present ton). The stone is still used to a considerable extent in Great Britain, being now equal to 14 pounds except in special cases. (8 stones = 1 hundredweight = 112 lb; 20 hundredweights = 1 ton = 2 240 lb. This ton is commonly referred to as the long ton in the United States.)

A unit of antiquity which has survived without change is the degree of arc. The early Babylonians reckoned the year as 360 days. They therefore divided the circle into 360 parts, or degrees. They knew that a chord equal to the radius subtends an arc of  $60^{\circ}$ . The number 60 became the basis of their sexagesimal number system and is an explanation of the division of the degree into 60 minutes and of the minute into 60 seconds. This is also the basis of the

relation between longitude and time. Since the earth makes one complete rotation (360°) on its axis in 24 hours, a time change of 1 hour is represented by each 15° of longitude (360/24 = 15).

#### 2.2. The Metric System

## a. The Metric System: Definition, Origin, and Development

The metric system is the international decimal system of weights and measures based on the meter and the kilogram. The essential features of the system system were embodied in a report made to the French National Assembly by the Paris Academy of Sciences in 1791. The definitive action taken in 1791 was the outgrowth of recommendations along similar lines dating back to 1670. The adoption of the system in France was slow, but is desirability as an international system was recognized by geodesists and others. On May 20, 1875, an international treaty known as the International Metric Convention was signed providing for an International Bureau of Weights and Measures, thus insuring 'the international unification and improvement of the metric system." The metric system is now either obligatory or permissive in every civilized country of the world.

Although the metric system is a decimal system, the words "metric" and "decimal" are not synonymous, and care should be taken not to confuse the two terms.

## b. Units and Standards of the Metric System

In the metric system the fundamental units are the meter and the kilogram. The other units of length and mass, as well as all units of area, volume, and capacity, also compound units, such as pressure, are derived from these two fundamental units.

The meter was originally intended to be 1 ten-millionth part of a meridional quadrant of the earth. The Meter of the Archives, the platinum end-standard which was the standard for most of the 19th century, at first was supposed to be exactly this fractional part of the quadrant. More refined measurements over the earth's surface showed that this supposition was not correct. The present international metric standard of length, the International Prototype Meter, a graduated line standard of platinum-iridium, was selected from a group of bars because it was found by precise measurements to have the same length as the Meter of the Archives. The meter is now defined as the distance under specified conditions between the lines on the International Prototype Meter without reference to any measurements of the earth or to the Meter of the Archives, which it superseded. The kilogram was originally intended to be the mass of one cubic decimeter of water at its maximum density, but it is now defined as the mass of the International Prototype Kilogram without reference to the mass of a cubic decimeter of water or to the Kilogram of the Archives. Each of the countries which subscribed to the International Metric Convention was assigned one or more copies of the international standards; these are known as National Prototype Meters and Kilograms. The liter is a unit of capacity based on the mass standard and is defined as the volume occupied, under standard conditions,

by a quantity of pure water having a mass of l kilogram. This volume is very nearly equal to l 000 cubic centimeters or l cubic decimeter; the actual metric equivalent is, l liter = l 000.028 cubic centimeters. (The change in this equivalent from the previously published value of l 000.027 is based on a recomputation of earlier data carried out at the International Bureau of Weights and Measures.) Thus the milliliter and the liter are larger than the cubic centimeter and the cubic decimeter, respectively, by 28 parts in l 000 000; except for determinations of high precision, this difference is so small as to be of no consequence.

The metric system, by itself, is not a complete system covering all physical measurements. A complete system requires certain additional units such, for example, as units of temperature and time.

## c. The International Bureau of Weights and Measures

The International Bureau of Weights and Measures was established at Sèvres, a suburb of Paris, France, in accordance with the International Metric Convention of May 20, 1875. At the Bureau there are kept the International Prototype Meter and the International Prototype Kilogram, many secondary standards of all sorts, and equipment for comparing standards and making precision measurements. The Bureau, maintained by assessed contributions of the signatory governments, is truly international.

In recent years the scope of the work at the International Bureau has been considerably broadened. It now carries on researches in the fields of electricity and photometry in addition to its former work in weights and measures with which were included such allied fields and thermometry and the measurement of barometric pressures.

## d. Present Status of the Metric System in the United States

The use of the metric system in this country was legalized by Act of Congress in 1866, but was not made obligatory.

The United States Prototype Meter No. 27 and United States Prototype Kilogram No. 20 are recognized as the primary standards of length and mass for both the metric and the customary systems of measurement in this country because these standards are the most precise and reliable standards available. Obviously it is not possible to accept both a meter and a yard, and both a kilogram and a pound as "primary" standards, unless there is willingness to accept the possibility of continually changing the ratio between the corresponding units. In each case one must be accepted as the primary standard and the other derived therefrom by means of an accepted relation. In the United States the yard is defined in terms of the meter, and the pound in terms of the kilogram. There is in the United States no primary standard either of length or mass in the customary system.

The use of metric units in certain athletic events in this country is undoubtedly of considerable interest to many people. Initial action by the Amateur Athletic Union was taken in November 1932, when it adopted metric distances for track events to be run in athletic meets held under the jurisdiction of that organization. Metric units for track and field events were adopted by various athletic organizations but this movement soon began to lose ground. In 1951 the use of metric distances in track and field events on national championship programs held under AAU auspices was restricted to Olympic years. The book compiled by Julia Emily Johnsen entitled "Metric System" and published in 1926 by The H. W. Wilson Co., New York, N. Y., contains arguments for and against the metric system, as well as a bibliography.

#### 2.3. British and United States Systems of Weights and Measures

The implication is sometimes made that the systems of weights and measures in general use in the British Empire and those in general use in the United States are identical. It is true that the U. S. and the British inch are defined identically for scientific work, that they are practically identical in commercial usage, that a similar situation exists for the U. S. and the British pound, and that many tables, such as 12 inches = 1 foot, 3 feet = 1 yard, and 1760 yards = 1 mile, are the same in both countries; but there are some very important differences.

In the first place, the U. S. bushel and the U. S. gallon, and their subdivisions differ from the corresponding British units. Also the British ton is 2 240 pounds, whereas the ton generally used in the United States is the short ton of 2 000 pounds. The American colonists adopted the English wine gallon of 231 cubic inches. The English of that period used this wine gallon and they also had another gallon, the ale gallon of 282 cubic inches. In 1824 these two gallons were abandoned by the British when they adopted the British Imperial gallon, which is defined as the volume of 10 pounds of water, at a temperature of 62°F, which, by calculation, is equivalent to 277.42 cubic inches. At the same time, the bushel was redefined as 8 gallons. In the British system the units of dry measure are the same as those of liquid measure. In the United States these two are not the same, the gallon and its subdivisions being used in the measurement of liquids, while the bushel, with its subdivisions, is used in the measurement of certain dry commodities. The U.S. gallon is divided into 4 liquid quarts and the U. S. bushel into 32 dry quarts. All the units of capacity mentioned thus far are larger in the British system than in the U.S. system. But the British fluid ounce is smaller than the U. S. fluid ounce, because the British quart is divided into 40 fluid ounces whereas the U. S. quart is divided into 32 fluid ounces.

From the foregoing it is seen that in the British system an avoirdupois ounce of water at 62°F has a volume of 1 fluid ounce, because 10 pounds is equivalent to 160 avoirdupois ounces, and 1 gallon is equivalent to 4 quarts, or 160 fluid ounces. This convenient relation does not exist in the U. S. system because a U. S. gallon of water at 62°F weighs about 8 1/3 pounds, or 133 1/3 avoirdupois ounces, and the U. S. gallon is equivalent to 4 x 32, or 128 fluid ounces.

> 1 U. S. fluid ounce = 1.040 8 British fluid ounces. 1 British fluid ounce = 0.960 8 U. S. fluid ounce.

Among other differences between the British and the American systems of weights and measures it should be noted that the use of the troy pound was abolished in England January 6, 1879, only the troy ounce and its subdivisions being ratained, whereas the troy pound is still legal in the United States, although it is not now greatly used. The common use in England of the stone of 14 pounds should be mentioned, this being a unit now unused in the United States, although its influence was shown in the practice until World War II of selling flour by the barrel of 196 pounds (14 stones). In the apothecaries system of liquid measure the British insert a unit, the fluid scruple, equal to one third of a fluid drachm (spelled dram in the United States) between their minim and their fluid drachm. In the United States the general practice now is to sell dry commodities, such as fruits and vegetables, by weight.

#### 2.4. Subdivision of Units

In general, units are subdivided by one of three systems: (a) decimal, that is into tenths; (b) duodecimal, into twelfths; or (c) binary, into halves. Usually the subdivision is continued by the use of the same system. Each method has its advantages for certain purposes and it cannot properly be said that any one method is "best" unless the use to which the unit and its subdivisions are to be put is known.

For example, if we are concerned only with measurements of length to moderate precision, it is convenient to measure and to express these lengths in feet, inches, and binary fractions of an inch, thus 9 feet 4 3/8 inches. If, however, these measured lengths are to be subsequently used in calculations of area or volume, that method of subdivision at once becomes extremely inconvenient. For that reason civil engineers, who are concerned with areas of land, volumes of cuts, fills, excavations, etc., instead of dividing the foot into inches and binary subdivisions of the inch, divide it decimally, that is, into tenths, hundredths, and thousandths of a foot.

The method of subdivision of a unit is thus largely made on the basis of convenience to the user. The fact that units have commonly been subdivided into certain subunits for centuries does not preclude these also having another mode of subdivision in some frequently used cases where convenience indicates the value of such other method. Thus the gallon is usually subdivided into quarts and pints, but the majority of gasoline-measuring pumps of the price-computing type are graduated to show tenths of a gallon. Although the mile has for centuries been divided into rods, yards, feet, and inches, the odometer part of an automobile speedometer indicates tenths of a mile. Although our dollar is divided into 100 parts, we habitually use and speak of halves and quarters. An illustration of rather complex subdividing is found on the scales used by draftsmen. These scales are of two types: (a) architects, which are commonly graduated with scales in which 3/32, 3/16, 1/8, 1/4, 3/8, 1/2, 3/4, 1, 1 1/2, and 3 inches, respectively, represent 1 foot full scale, as well as having a scale graduated in the usual manner to 1/16 inch; and (b) engineers, which are commonly subdivided to 10, 20, 30, 40, 50, and 60 parts to the inch.

The dictum of convenience applies not only to subdivisions of a unit but also to multiples of a unit. Elevations of land above sea level are given in feet even though the height may be several miles; the height of aircraft above sea level as given by an altimeter is likewise given in feet, no matter how high it may be. On the other hand, machinists, toolmakers, gage makers, scientists, and others who are engaged in precision measurements of relatively small distances, even though concerned with measurements of length only, find it convenient to use the inch, instead of the tenth of a foot, but to divide the inch decimally to tenths, hundredths, thousandths, etc., even down to millionths of an inch. Verniers, micrometers, and other precision measuring instruments are usually graduated in this manner. Machinist scales are commonly graduated decimally along one edge and are also graduated along another edge to binary fractions as small as 1/64 inch. The scales with binary fractions are used only for relatively rough measurements.

It is seldom convenient or advisable to use binary subdivisions of the inch that are smaller than 1/64. In fact, 1/32-, 1/16-, or 1/8-inch subdivisions are usually preferable for use on a scale to be read with the unaided eye.

#### 2.5. Arithmetical Systems of Numbers

The subdivision of units of measurement is closely associated with arithmetical systems of numbers. The systems of weights and measures used in this country for commercial and scientific work, having many origins as has already been shown, naturally show traces of the various number systems associated with their origins and developments. Thus (a) the binary subdivision has come down to us from the Hindus, (b) the duodecimal system of fractions from the Romans, (c) the decimal system from the Chinese and Egyptians, some developments having been made by the Hindus, and (d) the sexagesimal system (division by 60) now illustrated in the subdivision of units of angle and of time, from the ancient Babylonians.

The suggestion is made from time to time that we should adopt a duodecimal number system and a duodecimal system of weights and measures. Another suggestion is for an octonary number system (a system with 8 as the basis instead of 10 in our present system or 12 in the duodecimal) and an octonary system of weights and measures. Such suggestions have certain theoretical merits, but are very impractical because it is now too late to modify our number system and unwise to have arbitrary enforcement of any single system of weights and measures. It is far better for each branch of science, industry, and commerce to be free to use whatever system has been found by experience best to suit its needs. The prime requisite of any system of weights and measures is that the units be definite. It is also important that the relations of these units to the units of other systems be definite, convenient, and known, in order that conversio from one system to another may be accurately and conveniently made.

## 3. Standards of Length, Mass, Time, and Capacity

#### 3.1. Standards of Length

The primary standard of length in the United States is the United States Prototype Meter 27, a platinum-iridium (90% platinum, 10% iridium) line standard having an X-shaped cross section. The length of this bar, which is deposited at the National Bureau of Standards in Washington, is known in terms of the Intenational Prototype Meter at the International Bureau of Weights and Measures at Sèvres, near Paris, France. The yard is defined<sup>1</sup> as follows:

The inch is therefore exactly equal to 25.4 millimeters.

In 1927 the Seventh General (International) Conference on Weights and Measures approved a resolution stating the wavelength of the red cadmium radiation under standard conditions of temperature, pressure, and humidity to be 0.000 643 846 96 millimeter. From this the length of the meter in terms of the wavelength of light was provisionally expressed as equal to 1 553 164.13 wavelengths of cadmium light under the specified conditions.

With the advances made in physics in recent years better sources of monochromatic radiation for use as wavelength standards of length have been developed. The wavelength of the orange light from Krypton 86 is the proposed international standard on which all measurements will be based, subject to final adoption by the International Conference on Weights and Measures in 1960. To obtain a constant and uniform wavelength, Krypton lamps are operated at the temperature of the triple point of nitrogen.

Even after adoption of the Krypton standard, the more convenient green line of Hg 198 will serve as a working wavelength standard. Excited by highfrequency electric fields, it provides a very sharp spectral line, even at room temperature. Developed at the Eureau in 1947, Mercury 198 lamps are used as working standards in Taboratories throughout the world.

# a. Tests and Calibrations of Length Standards

The National Eureau of Standards tests standards of length including meter bars, yard bars, miscellaneous precision line standards, steel tapes, invar geodetic tapes, precision gage blocks, micrometers, and limit gages. It also measures the linear dimensions of miscellaneous apparatus such as penetration needles, cement sieves, and haemacytometer chambers. In general the Eureau accepts for test only apparatus of such material, design, and construction as to ensure accuracy and permanence sufficient to justify test by the Eureau. Tests are made in accordance with test-fee schedules, copies of which may be obtained by application to the Eureau.

The Eureau does not test carpenters rules, machinists scales, draftsmans scales, and the like. Such apparatus, if test is required, should be submitted to State or local weights and measures officials. NBS Monograph 15, Calibration of Line Standards of Length and Measuring Tapes at the National Bureau of Standards, by Lewis V. Judson, contains additional information on this subject.

## 3.2. Standards of Mass

The primary standard of mass for this country is United States Prototype Kilogram 20, which is a platinum-iridium standard kept at the National Bureau of Standards. The value of this mass standard is known in terms of the Inter-

See Federal Register for July 1, 1959.

national Prototype Kilogram, a platinum-iridium standard which is kept at the International Bureau of Weights and Measures.

For many years the British standards were considered to be the primary standards of the United States. Later, for over 50 years, the U. S. avoirdupois pound was defined in terms of the Troy Pound of the Mint, which is a brass standard kept at the United States Mint in Philadelphia. In 1911 the Troy Pound of the Mint was superseded, for coinage purposes, by the Troy Pound of the National Bureau of Standards. The avoirdupois pound is defined in terms of the Kilogram by the relation:

l avoirdupois pound - 0.453 592 37 kilogram.

These changes in definition have not made any appreciable change in the value of the pound.

The grain is  $1/7\ 000$  of the avoirdupois pound and is identical in the avoirdupois, troy, and apothecaries systems. The troy ounce and the apothecaries ounce differ from the avoirdupois ounce but are equal to each other, and equal to 480 grains. The avoirdupois ounce is equal to 437 1/2 grains.

## a. Distinction Between Mass and Weight

The mass of a body is a measure of its inertial property. The weight of a body is the force with which it is attracted by the earth. Confusion of these concepts arises because of our use of the terms kilogram, gram, pound, etc., in two different senses. The International Conference on Weights and Measures has defined the International Kilogram as a standard of mass, and consequently standards such as the pound and gram which are derived from it should be regarded as standards of mass also. However, common practice has also permitted use of the terms kilogram, gram, pound, etc., to designate the weights of these standards. This has been convenient because two bodies having equal masses also have equal weights under identical conditions, since the attraction of the earth for both of them is the same. Thus, standards of mass can also be used as standards of weight.

So long as no material is added to or taken from a body its mass remains constant. Its weight, however, varies with the acceleration of gravity,  $\underline{g}$ . For example, a body would be found to weigh more at the poles of the earth than at the equator, and less at high elevations than at sea level. (Standard acceleration of gravity, adopted by the International Committee on Weights and Measures in 1901 is 980.665 cm/sec<sup>2</sup>. This value corresponds nearly to the value at latitude 45° and sea level.)

Because standards of mass (or "weights") are ordinarily calibrated and used on equal-arm balances the effects of variations in the acceleration of gravity are self-eliminating and need not be taken into account. Two objects of equal mass will be affected in the same manner and by the same amount by any change in the value of the acceleration of gravity, and thus if they have the same weight, i.e., if they balance each other on an equal-arm balance, under one value of g, they will also balance each other under any other value of g. On a spring balance, however, the weight of the body is not balanced against the weight of another body, but against the restoring force of a spring. Therefore, using a very sensitive spring balance, the weight of a body would be found to change if the spring balance and the body were moved from one locality to another locality with a different acceleration of gravity. But a spring balance is usually used in one locality and is adjusted to indicate mass at that locality.

## b. Effect of Air Buoyancy

Another point that must be taken into account in the calibration and use of standards of mass is the buoyancy or lifting effect of the air. A body immersed in any fluid is buoyed up by a force equal to the weight of the displaced fluid. Two bodies of equal mass, if placed one on each pan of an equal-arm balance, will balance each other in a vacuum. A comparison in a vacuum against a known mass standard gives "true mass." If compared in air, however, they will not balance each other unless they are of equal volume. If of unequal volume, the larger body will displace the greater volume of air and will be buoyed up by a greater force than will the smaller body, and the larger body will appear to be lighter in weight than the smaller body. The greater the difference in volume, and the greater will be the apparent difference in weight. For that reason, in assigning a precise numerical value of apparent mass to a standard, it is necessary to base this value on definite values for the air density and the density of the mass standard of reference.

The corrections furnished by the National Eureau of Standards for the more precise mass standards are given both (a) on the basis of comparison in vacuum, and (b) on the basis of comparison against normal brass standards in air under standard conditions, with no correction applied for the buoyant effect of the air. Normal brass standards are defined as having a density of 8.4 grams per cubic centimeter at 0°C and a coefficient of cubical thermal expansion of 0.000 054 per deg C. Standard conditions are defined as air of 1.2 milligrams per cubic centimeter and temperature of 20°C. The corrections to be used with precise analytical weights are ordinarily given only in terms of apparent mass against normal brass standards.

#### c. Tests of Standards of Mass

Weights regularly used in ordinary trade and industry should be tested by State or local weights and measures officials. The National Bureau of Standards calibrates and certifies the values of weights submitted but it does not manufacture or sell weights. Information regarding the various classes of weights, the requirements for each class, the weight-calibration service of the Eureau and the regulations governing the submission of weights to NBS for test are contained in NES Circular 547, section 1, Precision Laboratory Standards of Mass and Laboratory Weights, by T. W. Lashof and L. B. Macurdy (for sale by the Superintendent of Documents, U. S. Government Printing Office, Washington 25, D. C., at 35 cents a copy).

#### 3.3. Standards of Time

There is no physical standard of time corresponding to the standards of length and mass. Time is measured in terms of the motion of the earth; (a) on its axis, and (b) around the sun. The time it takes the earth to make a complete rotation on its axis is called a day, and the time it takes it to make a complete journey around the sun, as indicated by its position with reference to the stars, is called a year. The earth makes about 366 1/4 rotations on its axis (366.242 2, more exactly) while making a complete journey around the sun. In other words, there are almost exactly 365 1/4 solar days in a tropical or solar year. As it would be inconvenient and confusing to have the year, as used in everyday life, contain a fractional part of a day, fractional days are avoided by making the calendar year contain 365 days in ordinary years and 366 days in leap years. The frequency of occurrence of leap years is such as to keep the average length of the calendar year as nearly as practicable equal to that of the tropical year, in order that calendar dates may not drift through the various seasons of the tropical year.

The earth, in its motion around the sun, does not move at a uniform speed, and the sun in its apparent motion does not move along the equator but along the ecliptic. Therefore the apparent solar days are not of exactly equal length. To overcome this difficulty time is measured in terms of the motion of a fictitious or "mean" sun, the position of which, at all times, is the same as would be the apparent position of the real sun if the earth moved on its axis and in its journey around the sun at a uniform rate. Ordinary clocks and watches are designed and regulated to indicate time in terms of the apparent motion of this fictitious or "mean sun." It is "mean noon" when this "mean sun" crosses the meridian, and the time between two successive crossings is a "mean solar day." The length of the mean solar day is equal to the average length of the apparent solar day.

In observing on the stars, the time generally used by astronomers is sidereal time. This is defined by the rotation of the earth with respect to the stars. A sidereal day is the interval between two successive passages of a star across a meridian. The sidereal day is subdivided into hours, minutes, and seconds, the hours being numbered from 1 to 24. The sidereal year is 365.256 35 solar days.

The mean solar day is divided into 24 hours, each hour into 60 minutes, and each minute into 60 seconds. Thus the mean solar second is 1/86400 of a mean solar day. Eecause the rotation of the earth on its axis varies slightly from time to time the second has been defined more exactly in terms of the revolution of the earth about the sun as 1/31 556 925.974 7 of the tropical year at 1900.0, 12 hours ephemeris time. At the beginning of 1960 this "ephemeris second" was shorter than the mean solar second by a little more than 1 part in 100 000 000.

The time at which the "mean sun" crosses the meridian at any point on the earth is known as "local mean noon." As it would be impracticable to use local mean time at each locality, the surface of the earth, by international agreement, has been divided into 24 standard time zones, each zone having a width of approximately 15 degrees of longitude. In each zone the time used is that corresponding to the meridian passing approximately through its center, and adjacent zones have a time difference of 1 hour. The meridian passing through Greenwich, England, is taken as the standard, or prime meridian, and time throughout the world is reckoned with reference to the time at Greenwich. Each 15 degrees east or west from Greenwich corresponds to a time difference of 1 hour. There are a few exceptions to the above rule. Clocks set to local time indicate later hours if east of Greenwich and earlier hours if west of Greenwich.

The contiguous states of the United States are in four time zones designated as Eastern, Central, Mountain, and Pacific. The time in these zones is earlier than Greenwich time by 5, 6, 7, and 8 hours, respectively. There are 4 additional time zones to cover Alaska and Hawaii: Yukon, Alaskan-Hawaiian, Bering, and Aleutian. These zones are earlier than Greenwich time by 9, 10, 11, and 12 hours, respectively.

Time and frequency are distributed to interested users by means of broadcasts of NBS Radio Stations WWV and WWVH at Beltsville, Maryland, and Puunene, Hawaii. The frequencies of these stations are kept in agreement with respect to each other and are maintained as constant as possible with respect to the United States Frequency Standard, which is a cesium resonator. The nominal broadcast frequencies should, for the purpose of highly accurate scientific measurements, for establishing high uniformity among frequencies, or for removing unavoidable variations in the broadcast frequencies, be corrected either to the United States Frequency Standard, as indicated in published monthly tables, or to a particular time scale as determined by the Naval Observatory, with adequate limits assigned for propagation errors.

#### 3.4. Standards of Capacity

Units of capacity, being derived units, in this country defined in terms of linear units, are not represented by fundamental standards. Laboratory standards have been constructed and are maintained at the National Bureau of Standards. These have validity only by calibration with reference either directly or indirectly with the linear standards. Similarly, standards of capacity have been made and distributed to the several States. Other standards of capacity have been verified by calibration for a wide variety of uses in science, technology, and commerce.

## a. Tests of Standards of Capacity

Calibrations are made by the Eureau on capacity standards that are in the customary units of trade, that is the gallon, its multiples, and submultiples, or in metric units. Furthermore the Bureau calibrates precision grade volumetric glassware which is normally in metric units. Tests are made in accordance with test-fee schedules, copies of which may be obtained by application to the Bureau.

3.5. Maintenance and Preservation of Fundamental Standards of Length and Mass

There is considerable interest in the maintenance and preservation of the national standards of length and mass at the National Bureau of Standards. In

1955, a special glass door, fully protected by an alarm system, was installed so that during the regular working hours of the Bureau the vault can be viewed by those interested. At other times the steel outer doors are locked. All measurements made with these standards are conducted in special air-conditioned laboratories to which the standards are taken a sufficiently long time before the observations to ensure that the standards will be in a state of equilibrium under standard conditions when the measurements or comparisons are made. Hence it is not necessary to maintain the vault at standard conditions, but care is taken to prevent large changes of temperature. More important is the care to prevent any damage to the standards because of careless handling.

## 4. Weights and Measures in Everyday Life

As weighing and measuring are important factors in our everyday lives, it is quite natural that questions arise about the use of various units and terms and about the magnitude of quantities involved. For example, the words "ton" and "tonnage" are used in widely different senses, and a great deal of confusion has arisen regarding the application of these terms.

The ton is used as a unit of measure in two distinct senses: (1) as a unit of weight, and (2) as a unit of capacity or volume.

In the first sense the term has the following meanings:

- (a) The short, or net ton to 2 000 pounds.
- (b) The long, gross, or shipper's ton of 2 240 pounds.
- (c) The metric ton of 1 000 kilograms, or 2 204.6 pounds.

In the second sense (capacity) it is usually restricted to uses relating to ships and has the following meaning:

- (a) The register ton of 100 cubic feet.(b) The measurement ton of 40 cubic feet.
- (c) The English water ton of 224 British Imperial gallons.

In the United States and Canada the ton (weight) most commonly used is the short ton, in Great Britain it is the long ton, and in countries using the metric system it is the metric ton. The register ton and the measurement ton are capacity units used in expressing the tonnage of ships. The English water ton is used, chiefly in Great Britain, in statistics dealing with petroleum products.

There have been many other uses of the term ton such as the timber ton of 40 cubic feet and the wheat ton of 20 bushels, but their use has been local and the meanings have not been consistent from one place to another.

Properly, the word "tonnage" is used as a noun only in respect to the capacity and dimensions of ships, and to the amount of the ship's cargo. There are two distinct kinds of tonnage, namely, vessel tonnage and cargo tonnage and each of these is used in various meanings.

The several kinds of vessel tonnage are as follows:

Gross tonnage, or gross register tonnage, is the total cubical capacity of a ship expressed in register tons of 100 cubic feet, or 2.83 cubic meters, less such space as hatchways, bakeries, galleys, etc., as are exempted from measurement by different governments. There is some lack of uniformity in the gross tonnages as given by different nations on account of lack of agreement on the spaces that are to be exempted.

Official merchant marine statistics of most countries are published in terms of the gross register tonnage. Press references to ship tonnage are usually to the gross tonnage.

The net tonnage, or net register tonnage, is the gross tonnage less the different spaces specified by maritime nations in their measurement rules and laws. The spaces that are deducted are those totally unavailable for carrying cargo, such as the engine room, coal bunkers, crews quarters, chart and instrument room, etc.

The net tonnage is used in computing the amount of cargo that can be loaded on a ship. It is used as the basis for wharfage and other similar charges.

The register under-deck tonnage is the cubical capacity of a ship under her tonnage deck expressed in register tons. In a vessel having more than one deck the tonnage deck is the second from the keel.

There are several variations of displacement tonnage.

The <u>dead weight tonnage</u> is the difference between the "loaded" and "light" <u>displacement tonnages</u> of a vessel. It is expressed in terms of the long ton of 2 240 pounds, or the metric ton of 2 204.6 pounds, and is the weight of fuel, passengers, and cargo that a vessel can carry when loaded to her maximum draft.

The second variety of tonnage, <u>cargo tonnage</u>, refers to the weight of the particular items making up the cargo. In overseas traffic it is usually expressed in long tons of 2 240 pounds or metric tons of 2 204.6 pounds. The short ton is only occasionally used. The <u>cargo tonnage</u> is therefore very distinct from vessel tonnage.

### 5. General Tables of Weights and Measures

These tables have been prepared for the benefit of those requiring tables of weights and measures for occasional ready reference. In section 5.4 the tables are carried out to a large number of decimal places and exact values are indicated by underlining. In most of the other tables only a limited number of decimal places are given, thus making the tables better adapted to the average user. More extensive tables will be found in a Miscellaneous Publication of the National Bureau of Standards, Units of Weight and Measure --Definitions and Tables of Equivalents (sold by the Superintendent of Documents, U. S. Government Printing Office, Washington 25, D. C. (now temporarily out of print). 5.1. Tables of United States Customary Weights and Measures

## LINEAR MEASURE

12 inches (in.)	= 1 foot (ft).
3 feet	= 1  yard (yd).
$5 \ 1/2 \ yards$	= 1 rod (rd), pole, or perch = $16 1/2$ feet.
40 rods	= 1 furlong (fur.) = 220 yards - 660 feet.
8 furlongs	= 1 statute mile (mi) = 1 760 yards = 5 280 feet.
$1\ 852\ meters = 6\ 076.\ 115\ 49$	feet (approximately) = 1 international nautical mile.

AREA MEASURE<sup>a</sup>

144	square inches (sq in.)	= 1	square foot (sq ft).
9	square feet	= 1	square yard (sq yd) = 1 296 square inches.
30	1/4 square yards	= 1	square rod (sq rd) = 272 1/4 square feet.
160	square rods	= 1	acre = 4 840 square yards = 43 560 square feet.
640	acres	= 1	square mile (sq mi).
1	mile square	= 1	section of land.
6	miles square	= 1	township = 36 sections - 36 square miles.

# CUBIC MEASURE<sup>a</sup>

1 728 cubic inches (cu in.) = 1 cubic foot (cu ft). 27 cubic feet = 1 cubic yard (cu yd).

GUNTER'S OR SURVEYORS CHAIN MEASURE

7.92 inches (in.)	_=	1	link (li).			
100 link <b>s</b>	Ξ	1	chain (ch) = 4 rods	= 66 feet.		
80 chains	=	1	statute mile (mi) -	320 rods - 5	280	feet.

# LIQUID MEASURE<sup>b</sup>

```
4 gills (gi) = 1 pint (pt) - 28.875 cubic inches.

2 pints = 1 quart (qt) = 57.75 cubic inches.

4 quarts = 1 gallon (gal) = 231 cubic inches = 8 pints = 32 gills.
```

<sup>a</sup>Squares and cubes of units are sometimes abbreviated by using "superior" figures. For example, ft<sup>2</sup> means square foot, and ft<sup>3</sup> means cubic foot.

<sup>b</sup>When necessary to distinguish the <u>liquid</u> pint or quart from the <u>dry</u> pint or quart, the word "liquid" or the abbreviation "liq" should be used in combination with the name or abbreviation of the liquid unit.

#### APOTHECARIES FLUID MEASURE

60	minims (min o	$\operatorname{or} \mathfrak{M} = 1$	fluid dram (fl dr or $f$ <b>3</b> ) = 0.225 6 cubic inch.
8	fluid drams	= 1	fluid ounce (fl oz or $f$ 3) = 1.804 7 cubic inches.
16	fluid ounces	= 1	pint (pt or O) = 28.875 cubic inches = 128 fluid drams.
2	pints	= 1	quart (qu) = 57.75 cubic inches = 32 fluid ounces = 256 fluid drams.
4	quarts	= 1	gallon (gal) = 231 cubic inches = 128 fluid ounces =
	*		1 024 fluid drams.

DRY MEASURE<sup>C</sup>

```
2 pints (pt) = 1 quart (qt) = 67.200 6 cubic inches.
8 quarts = 1 peck (pk) = 537.605 cubic inches = 16 pints.
4 pecks = 1 bushel (bu) = 2 150.42 cubic inches = 32 quarts.
```

AVOIRDUPOIS WEIGHT<sup>d</sup>

[The "grain" is the same in avoirdupois, troy, and apothecaries weight.]

27	11/32 grains	= 1	dram (dr).
16	drams	= 1	ounce $(oz) = 437 1/2$ grains.
16	ounces	= 1	pound (1b) = 256 drams = 7 000 grains.
100	pounds	= 1	hundredweight (cwt). <sup>e</sup>
20	ĥundredweights	= 1	ton = 2 000 pounds. $e$

In "gross" or "long" measure, the following values are recognized:

112 pounds = 1 gross or long hundredweight. <sup>e</sup> 20 gross or long hundredweights = 1 gross or long ton = 2 240 pounds. <sup>e</sup>

#### TROY WEIGHT

[The "grain" is the same in avoirdupois, troy, and apothecaries weight.]

```
24 grains = 1 pennyweight (dwt).
20 pennyweights = 1 ounce troy (oz t) = 480 grains.
12 ounces troy = 1 pound troy (lb t) = 240 pennyweights = 5 760 grains.
```

<sup>C</sup>When necessary to distinguish the <u>dry</u> pint or quart from the <u>liquid</u> pint or quart, the word "dry" should be used in combination with the name or abbreviation of the dry unit.

<sup>d</sup>When necessary to distinguish the <u>avoirdupois</u> dram from the <u>apothecaries</u> dram, or to distinguish the <u>avoirdupois</u> dram or ounce from the <u>fluid</u> dram or ounce, or to distinguish the <u>avoirdupois</u> ounce or pound from the troy or <u>apothecaries</u> ounce or pound, the word "avoirdupois" or the abbreviation "avdp" should be used in combination with the name or abbreviation of the avoirdupois unit.

<sup>e</sup>When the terms "hundredweight" and "ton" are used unmodified, they are commonly understood to mean the 100-pound hundredweight and the 2 000-pound ton, respectively; these units may be designated "net" or "short" when necessary to distinguish them from the corresponding units in gross or long measure.

#### APOTHECARIES WEIGHT

[The "grain" is the same in avoirdupois, troy, and apothecaries weight.]

20	grains	=	1	scruple (s ap or $\mathfrak B$ ).
3	scruples	=	1	dram apothecaries (dr ap or $3$ ) = 60 grains.
8	drams apothecaries	=	1	ounce apothecaries (oz ap or $3$ ) = 24 scruples =
				480 grains.
12	ounces apothecaries	=	1	pound apothecaries (lb ap or 1b) = 96 drams apothe-
				caries = 288 scruples = 5 760 grains.

## 5.2. Notes on British Weights and Measures Tables

In Great Britain, the yard, the avoirdupois pound, the troy pound, and the apothecaries pound, are, for all commercial purposes, identical with the units of the same names used in the United States. The tables of British linear measure, troy weight, and apothecaries weight are the same as the corresponding United States tables, except for the British spelling "drachm" in the table of apothecaries weight. The table of British avoirdupois weight is the same as the United States table up to 1 pound; above that point the table reads:

14	pounds	=	1	stone.
2	<b>s</b> tone <b>s</b>	=	1	quarter = 28 pounds.
4	quarters	=	1	hundredweight = 112 pounds.
20	hundredweight	=	1	ton = $2240$ pounds.

The present British gallon and bushel, known as the "Imperial gallon" and "Imperial bushel" are, respectively, about 20 percent and 3 percent larger than the United States gallon and bushel. The Imperial gallon is defined as the volume of 10 avoirdupois pounds of water under specified conditions, and the Imperial bushel is defined as 8 Imperial gallons. Also, the subdivision of the Imperial gallon as presented in the table of British apothecaries fluid measure differs in two important respects from the corresponding United States subdivision, in that the Imperial gallon is divided into 160 fluid ounces (whereas the United States gallon is divided into 128 fluid ounces), and a "fluid scruple" is included. The full table of British measures of capacity (which are used alike for liquid and for dry commodities) is as follows:

4	gills	Ξ	1	pint.
2	pints	=	1	quart.
4	quarts	=	1	gallon.
2	gallons	=	1	peck.
8	gallons [4 pecks]	=	1	bushel.
8	bushels	=	1	quarter.

The full table of British apothecaries measure is as follows:

20	minims	= 1	fluid scruple.
3	fluid scruples	= 1	fluid drachm = 60 minims.
8	fluid drachms	= 1	fluid ounce.
20	fluid ounces	= 1	pint.
8	pints	= 1	gallon = 160 fluid ounces.

#### 5.3. Tables of Metric Weights and Measures

In the metric system of weights and measures, designations of multiples and subdivisions of any unit may be arrived at by combining with the name of the unit the prefixes deka, hecto, and kilo, meaning, respectively, 10, 100, and 1 000, and deci, centi, and milli, meaning, respectively, one-tenth, onehundredth, and one-thousandth. In some of the following metric tables, some such multiples and subdivisions have not been included for the reason that these have little, if any currency in actual usage.

In certain cases, particularly in scientific usage, it becomes convenient to provide for multiples larger than 1 000 and for subdivisions smaller than one-thousandth. Accordingly, the following prefixes have been introduced and these are now generally recognized:

tera,	meaning	1012	pico,	meaning	10-12
giga,	meaning	109	nano,	meaning	10-9
mega,	meaning	106	micro,	meaning	10-6
kilo,	meaning	103	milli,	meaning	10-3
hecto,	meaning	102	centi,	meaning	10 - 2
deka,	meaning	101	deci,	meaning	10-1

Thus a kilometer is 1 000 meters and a millimeter is 0.001 meter. These prefixes are appropriately applied to all kinds of units and retain their significance as in kilowatts, picofarads, megacycles, and microinches. A special case is found in the term "micron" (abbreviated as  $\mu$ , the Greek letter mu), a coined word meaning one-millionth of a meter (equivalent to one-thousandth of a millimeter.) Although the above prefixes now replace the millimicron and the micromicron, these terms are still found in the literature. A millimicron (abbreviated as  $m\mu$ ) is one-thousandth of a micron (equivalent to one-millionth of a millimeter), and a micromicron (abbreviated as  $\mu\mu$ ) is one-thousandth of a millimeter).

## LINEAR MEASURE

10	millimeters (mm)	= 1	centimeter (cm).
10	centimeters	= 1	decimeter (dm) = 100 millimeters.
10	decimeters	= 1	meter (m) = 1 000 millimeters.
10	meters	= 1	dekameter (dkm).
10	dekameters	= 1	hectometer (hm) = 100 meters.
10	hectometers	= 1	kilometer (dm) = 1 000 meters.

#### AREA MEASURE

	100 square	e millimeters	$(mm^2) = 1$	square centimeter (cm <sup>2</sup> ).
10	000 square	e centimeters	= 1	square meter $(m^2) = 1\ 000\ 000$ square millimeters.
	100 square	e meters	= 1	are (a).
	100 ares		= 1	hectare (ha) = 10 000 square meters.
	100 hectar	es	= 1	square kilometer (km <sup>2</sup> ) = 1 000 000 square meters.

## VOLUME MEASURE

10	milliliters (ml)	= 1	centiliter (cl).
10	centiliters	= 1	deciliter (dl) = 100 milliliters.
10	deciliters	= 1	liter <sup>f</sup> = 1 000 milliliters.
10	liters	= 1	dekaliter (dkl).
10	dekaliters	= 1	hectoliter (hl) = 100 liters.
10	hectoliters	= 1	kiloliter (kl) = 1 000 liters.

## CUBIC MEASURE

1	000	cubic	millimeters	$(mm^3) = 1$	l cubic centimeter (cm <sup>3</sup> ).
1	000	cubic	centimeters	= 1	l cubic decimeter ( $dm^3$ ) = 1 000 000 cubic
					millimeters.
1	000	cubic	decimeters	= 1	$1 \text{ cubic meter } (m^3) = 1 \text{ stere} = 1 000 000$
					cubic centimeters = 1 000 000 000 cubic
					millimeters.

## WEIGHT

	10 milligrams (mg)	= 1 centigram (cg).	
	10 centigrams	= 1 decigram (dg) = 100 milligrams.	
	10 decigrams	= 1 gram (g) = 1 000 milligrams.	
	10 grams	= 1 dekagram (dkg).	
	10 dekagrams	= 1 hectogram (hg) = 100 grams.	
	10 hectograms	= 1 kilogram (kg) = 1 000 grams.	
l	000 kilograms	= 1 metric ton (t).	

<sup>&</sup>lt;sup>f</sup>The liter is defined as the volume occupied, under standard conditions, by a quantity of pure water having a mass of 1 kilogram. This volume is very nearly equal to 1 000 cubic centimeters or 1 cubic decimeter; the actual metric equivalent is, 1 liter = 1 000.028 cubic centimeters. (The change in this equivalent from the previously published value of 1 000.027 is based on a recomputation of earlier data, carried out at the International Bureau of Weights and Measures.) Thus the milliliter and the liter are larger than the cubic centimeter and the cubic decimeter, respectively, by 28 parts in 1 000 000; except for determinations of high precision, this difference is so small as to be of no consequence.

## 5.4. TABLES OF INTERRELATION OF UNITS OF MEASUREMENT

Units	Inches	Links	Feet	Yards	Rods
l inch = l link = l foot = l yard = l rod = l chain = l mile = l centimeter = l meter =	$ \begin{array}{r}      \frac{1}{7.92} \\     \frac{12}{36} \\     \frac{198}{792} \\     \frac{63}{360} \\     \hline     0.3937008 \\     39.37008 \end{array} $	$\begin{array}{c} 0.126 \ 262 \ 6\\ 1.515 \ 152\\ 4.545 \ 45\\ \underline{25}\\ \underline{100}\\ 0.049 \ 709 \ 70\\ 4.970 \ 970 \end{array}$	$\begin{array}{c} 0.\ 083\ 333\ 33\\ \underline{0.\ 66}\\ \underline{1}\\ \underline{3}\\ \underline{16.5}\\ \underline{66}\\ \underline{5280}\\ 0.\ 032\ 808\ 40\\ 3.\ 280\ 840 \end{array}$	$\begin{array}{c} 0.\ 027\ 777\ 78\\ \underline{0.22}\\ 0.\ 333\ 333\ 3\\ \underline{5.5}\\ \underline{1760}\\ 0.\ 010\ 936\ 13\\ 1.\ 093\ 613 \end{array}$	$\begin{array}{cccccccc} 0.005 & 050 & 505 \\ \hline 0.04 \\ 0.060 & 606 & 06 \\ 0.181 & 818 & 2 \\ & & \frac{1}{4} \\ \hline & & \frac{320}{0} \\ 0.001 & 988 & 388 \\ 0.198 & 838 & 8 \end{array}$

#### UNITS OF LENGTH

Units	Chains	Miles	Centimeters	Meters
1 inch = 1 link = 1 foot = 1 yard = 1 rod = 1 chain = 1 mile = 1 centimeter = 1 meter =	$\begin{array}{c} 0.\ 001\ 262\ 626\\ \hline 0.\ 01\\ 0.\ 015\ 151\ 52\\ 0.\ 045\ 454\ 55\\ \hline 0.\ 25\\ \hline 1\\ 0.\ 000\ 497\ 097\ 0\\ 0.\ 049\ 709\ 70\\ \end{array}$	$\begin{array}{c} 0.\ 000\ 015\ 782\ 83\\ \hline 0.\ 000\ 125\\ \hline 0.\ 000\ 189\ 393\ 9\\ 0.\ 000\ 568\ 181\ 8\\ \hline 0.\ 003\ 125\\ \hline 0.\ 012\ 5\\ \hline \hline 0.\ 012\ 5\\ \hline \hline 0.\ 000\ 006\ 213\ 712\\ \hline 0.\ 000\ 621\ 371\ 2\\ \end{array}$	$     \begin{array}{r} 2.54 \\             \underline{20,116,8} \\             \underline{30,48} \\             \underline{91,44} \\             \underline{502,92} \\             \underline{2011,68} \\             \underline{160,934,4} \\             \underline{100} \\             \end{array}         $	$\begin{array}{c} \underline{0.\ 025\ 4}\\ \underline{0.\ 201\ 168}\\ 0.304\ 8\\ \hline 0.914\ 4\\ \underline{5.\ 029\ 2}\\ \underline{20.116\ 8}\\ \underline{1609.344}\\ \hline 0.01 \\ \hline \end{array}$

#### UNITS OF VOLUME

Units	Cubic Inches	Cubic Feet	Cubic Yards
l cubic inch = l cubic foot = l cubic yard = l cubic centimeter = l cubic decimeter = l cubic meter =	$\begin{array}{r} & \underline{1728} \\ & \underline{46\ 656} \\ & 0.\ 061 \\ \hline 023\ 74 \\ 61\ 023\ 74 \end{array}$	$\begin{array}{c} 0.000 578 703 7 \\ 1 \\ 27 \\ 0.000 035 314 67 \\ 0.035 314 67 \\ 35.314 67 \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

Units	Cubic Centimeters	Cubic Decimeters	Cubic Meters
l cubic inch = l cubic foot = l cubic yard = l cubic centimeter = l cubic decimeter = l cubic meter =	$ \begin{array}{r} 16.387064\\28316.846592\\764554.857984\\\underline{1000}\\\underline{1000000}\end{array} $	$\begin{array}{c} 0,016 \ 387 \ 064 \\ 28,316 \ 846 \ 592 \\ \hline 764,554 \ 857 \ 984 \\ \hline 0,001 \\ \hline & 1000 \\ \hline \end{array}$	$\begin{array}{c} 0.\ 000\ 016\ 387\ 064\\ 0.028\ 316\ 846\ 592\\ 0.\ 764\ 554\ 857\ 984\\ \hline 0.000\ 001\\ \hline \hline 0.\ 001 \\ \hline \end{array}$

- .

# UNITS OF AREA

Units	Square Inches	Square Links	Square Feet	Square Yards	Square Rods
<pre>l square inch = l square link = l square foot = l square yard = l square rod = l square chain = l acre = l square mile = l square centimeter = l square meter = l hectare =</pre>	$\begin{array}{r} \underline{1} \\ \underline{62.726.4} \\ \underline{1296} \\ \underline{39.204} \\ \underline{627.264} \\ \underline{6.272.640} \\ \underline{4.014.489.600} \\ \underline{0.155.000.3} \\ 1550.003 \\ \underline{15.500.031} \end{array}$	$\begin{array}{c} 0.015 \ 942 \ 25 \\ 2.295 \ 684 \\ 20.661 \ 16 \\ \hline 10 \ 000 \\ \underline{64 \ 000 \ 000} \\ 0.002 \ 471 \ 054 \\ 24.710 \ 54 \\ 247 \ 105 \ 4 \end{array}$	$\begin{array}{c} 0.006 \ 944 \ 444 \\ \underline{0.435 \ 6} \\ \underline{19} \\ \underline{272.25} \\ \underline{43560} \\ \underline{27 \ 878 \ 400} \\ 0.001 \ 076 \ 391 \\ 10.763 \ 91 \\ 107 \ 639.1 \end{array}$	$\begin{array}{c} 0.000 & 771 & 604 & 9 \\ \underline{0.048} & \underline{4} \\ 0.111 & 111 & 1 \\ \underline{30.25} & \underline{484} \\ \underline{4840} \\ 0.000 & \underline{3.097} & 600 \\ 0.000 & 119 & 599 & 0 \\ 1.195 & 990 \\ 11 & 959.90 \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

Units	Square Chains	Acres	Square Miles	
<pre>l square inch = l square link = l square foot = l square yard = l square rod = l square chain = l acre = l square mile = l square mile = l square meter = l hectare =</pre>	$\begin{array}{c} 0.000 \ 001 \ 594 \ 225 \\ \underline{0.000 \ 1} \\ 0.000 \ 229 \ 568 \ 4 \\ 0.002 \ 066 \ 116 \\ \underline{0.062 \ 5} \\ \underline{10} \\ \underline{6400} \\ 0.000 \ 000 \ 247 \ 105 \ 4 \\ 24.710 \ 54 \end{array}$	$\begin{array}{c} 0.\ 000\ 000\ 159\ 422\ 5\\ \hline 0.\ 000\ 01\\ \hline 0.\ 000\ 022\ 956\ 84\\ \hline 0.\ 000\ 206\ 611\ 6\\ \hline 0.\ 000\ 25\\ \hline 0.1 \\ \hline 0.\ 000\ 024\ 710\ 54\\ \hline 0.\ 000\ 247\ 105\ 4\\ \hline 2.\ 471\ 054 \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	

Units	Square Centimeters	Square Meters	Hectares
<pre>l square inch = l square link = l square foot = l square yard = l square rod = l square rod = l acre = l square mile = l square mile = l square meter = l hectare =</pre>	$\begin{array}{r} \underbrace{\begin{array}{r} \underline{6,451} & 6 \\ \underline{404,685} & 642 & 24 \\ \underline{929,030} & 4 \\ \underline{929,030} & 4 \\ \underline{8361,273} & 6 \\ \underline{4046} & 856,422 & 4 \\ \underline{4046} & 856,422 & 4 \\ \underline{4046} & 8564,224 \\ \underline{25} & 899 & 881 & 103.36 \\ \hline \\ \underline{100} & \underline{100} & \underline{100} \\ \hline \end{array}}$	$\begin{array}{c} \underbrace{\begin{array}{c} 0.000 & 645 & 16 \\ \hline 0.040 & 468 & 564 & 224 \\ \hline 0.092 & 903 & 04 \\ \hline 0.836 & 127 & 36 \\ \hline 25,292 & 852 & 64 \\ \hline 404.685 & 642 & 24 \\ \hline 4046.856 & 422 & 4 \\ \hline 2 & 589 & 988.110 & 336 \\ \hline 0.000 & 1 \\ \hline 10 & 000 \\ \hline \end{array}}$	$\begin{array}{c} 0.000 & 000 & 064 & 516 \\ \hline 0.000 & 004 & 046 & 856 & 422 & 4 \\ \hline 0.000 & 009 & 290 & 304 \\ \hline 0.000 & 083 & 612 & 736 \\ \hline 0.002 & 529 & 285 & 264 \\ \hline 0.040 & 468 & 564 & 224 \\ \hline 0.404 & 685 & 642 & 24 \\ \hline 258.998 & 811 & 033 & 6 \\ \hline 0.000 & 000 & 01 \\ \hline 0.000 & 1 \\ \hline \end{array}$

## UNITS OF CAPACITY LIQUID MEASURE

Units	Minims	Fluid Drams	Fluid Ounces	Gills
<pre>l minim = l fluid dram = l fluid ounce = l gill = l liquid pint = l gallon = l cubic inch = l cubic foot = l milliliter = l liter =</pre>	$\begin{array}{r} \begin{array}{r} 1 \\ 60 \\ 480 \\ 1920 \\ \hline 7680 \\ \hline 61 \\ 440 \\ 265 \\ 974 \\ 0 \\ 459 \\ 603.1 \\ 16.231 \\ 19 \\ 16 \\ 231.19 \end{array}$	$\begin{array}{c} 0.\ 016 \ \ 666 \ \ 67 \\ \\ \underline{32} \\ \underline{32} \\ \underline{128} \\ \underline{256} \\ \underline{1024} \\ 4.\ 432 \ 900 \\ 7660.\ 052 \\ 0.\ 270 \ \ 519 \ \ 8 \\ 270.\ 519 \ \ 8 \end{array}$	$\begin{array}{c} 0.\ 002 \ 083 \ 333 \\ \underline{0.125} \\ 1 \\ \underline{16} \\ 32 \\ 128 \\ 0.\ 554 \ 112 \ 6 \\ 957.\ 506 \ 5 \\ 0.\ 033 \ 814 \ 97 \\ 33.\ 814 \ 97 \end{array}$	$\begin{array}{c} 0.\ 000\ 520\ 833\ 3\\ \underline{0.\ 031\ 25}\\ \hline 0.\ 25\\ \hline 0.\ 0.\ 0.\ 0.\ 0.\ 0.\ 0.\ 0$

Units	Liquid Pints	Liquid Quarts	Gallons	Cubic Inches
l minim = l fluid dram = l fluid ounce = l gill = l liquid pint = l liquid quart= l gallon = l cubic foot = l milliliter = l liter =	$\begin{array}{c} 0.\ 000\ 130\ 208\ 3\\ \underline{0.\ 007\ 812\ 5}\\ \underline{0.\ 062\ 5}\\ \underline{0.\ 25}\\ \underline{0.\ 034\ 632\ 03}\\ 59.\ 844\ 16\\ 0.\ 002\ 113\ 436\\ 2.\ 113\ 436 \end{array}$	$\begin{array}{c} 0.000 & 065 & 104 & 17 \\ 0.003 & 906 & 25 \\ \hline 0.031 & 25 \\ \hline 0.5 \\ \hline 0.017 & 316 & 02 \\ 29.922 & 08 \\ 0.001 & 056 & 718 \\ 1.056 & 718 \end{array}$	$\begin{array}{c} 0.000 & 016 & 276 & 04 \\ 0.000 & 976 & 562 & 5 \\ \hline 0.007 & 812 & 5 \\ \hline 0.031 & 25 \\ \hline 0.25 \\ \hline 0.25 \\ \hline 0.004 & 329 & 004 \\ \hline 1.480 & 519 \\ 0.000 & 264 & 179 & 4 \\ \hline 0.264 & 179 & 4 \\ \hline \end{array}$	$\begin{array}{c} 0.003 & 759 & 766 \\ 0.225 & 585 & 94 \\ \underline{1.804 & 687 & 5} \\ \hline 7.218 & 75 \\ \underline{28.875} \\ \underline{57.75} \\ \underline{57.75} \\ \underline{1.128} \\ 0.061 & 025 & 45 \\ 0.025 & 45 \\ \end{array}$

Units	Cubic Feet	Milliliters	Liters
<pre>l minim = l fluid dram = l fluid ounce = l gill = l liquid pint = l liquid quart= l gallon = l cubic inch = l cubic foot = l milliliter = l liter =</pre>	$\begin{array}{c} 0.\ 000\ 002\ 175\ 790\\ 0.\ 000\ 130\ 547\ 4\\ 0.\ 001\ 044\ 379\\ 0.\ 004\ 177\ 517\\ 0.\ 016\ 710\ 07\\ 0.\ 033\ 420\ 14\\ 0.\ 133\ 680\ 6\\ 0.\ 000\ 578\ 703\ 7\\ 0.\ 000\ 035\ 315\ 66\\ 0.\ 035\ 315\ 66\\ \end{array}$	$\begin{array}{r} 0.\ 061\ 609\ 79\\ 3.\ 696\ 588\\ 29.\ 572\ 70\\ 118.\ 290\ 8\\ 473.\ 163\ 2\\ 946.\ 326\ 4\\ 3785.\ 306\\ 16.\ 386\ 61\\ 28\ 316.\ 05\\ \hline \begin{array}{r} 1\\ 1000\\ \hline \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

## UNITS OF CAPACITY DRY MEASURE

Units	Dry Pints	Dry Quarts	Pecks	Bushels
l dry pint = l dry quart = l peck = l bushel = l cubic inch = l cubic foot = l liter = l dekaliter =	$\begin{array}{r} \frac{1}{2}\\ \underline{16}\\ 64\\ 51,428&09\\ 1,816&217\\ 18,162&17 \end{array}$	$\begin{array}{c} \underline{0.5} \\ \underline{8} \\ \underline{32} \\ 0.014 \\ 880 \\ 8 \\ 25.714 \\ 0.908 \\ 108 \\ 4 \\ 9.081 \\ 084 \\ \end{array}$	$\begin{array}{c} \underline{0.062\ 5}\\ \underline{0.125}\\ 0.001\ 860\ \overline{10}\\ 3.214\ 256\\ 0.113\ 513\ 6\\ 1.135\ 136 \end{array}$	$\begin{array}{c} \underline{0.015} & \underline{625} \\ \underline{0.031} & \underline{25} \\ \hline \underline{0.25} & \underline{1} \\ 0.000 & 465 & 025 \\ 0.803 & 563 & 95 \\ 0.028 & 378 & 39 \\ 0.283 & 783 & 9 \end{array}$

Units	Cubic Inches	Cubic Feet	Liters	Dekaliters
<pre>l dry pint = l dry quart = l peck = l bushel = l cubic inch = l cubic foot = l liter = l dekaliter =</pre>	$\begin{array}{r} 33.600 312 5\\ \hline 67.200 625\\ \hline 537.605\\ \hline 2150.42\\ \hline \\ 61.025 45\\ 610.254 5\end{array}$	$\begin{array}{c} 0. \ 019 \ 444 \ 63 \\ 0. \ 038 \ 889 \ 25 \\ 0. \ 311 \ 114 \\ 1.244 \ 456 \\ 0. \ 000 \ 578 \ 703 \ 7 \\ \hline 1 \\ 0. \ 035 \ 315 \ 66 \\ 0. \ 353 \ 156 \ 6 \end{array}$	$\begin{array}{c} 0.550 595 1 \\ 1.101 190 \\ 8.809 521 \\ 35.238 08 \\ 0.016 386 61 \\ 28.316 053 73 \\ \underline{1} \\ 10 \end{array}$	0.055 059 51 0.110 119 0 0.880 952 1 3.523 808 0.001 638 661 2.831 605 0.1 1

#### UNITS OF MASS NOT LESS THAN AVOIRDUPOIS OUNCES

Units	Avoirdupois Ounces	Avoirdupois Pounds	Short Hundred- weights	Short tons
l avoirdupois ounce = l avoirdupois pound = l short hundredweight = l short ton = l long ton = l kilogram = l metric ton =	$\begin{array}{r} \begin{array}{r} 1\\ 16\\ \hline 1600\\ \hline 32000\\ \hline 35.840\\ \hline 35.27396\\ \hline 35.273.96 \end{array}$	$     \underbrace{\begin{array}{c}       0.0625 \\       \frac{100}{2.240} \\       2.204.623     \end{array}}     $	$\begin{array}{r} \underline{0.000 \ 625} \\ \underline{0.01} \\ \underline{1} \\ \underline{20} \\ \underline{22.4} \\ 0.022 \ 046 \ 23 \\ 22.046 \ 23 \end{array}$	$\begin{array}{c} 0.000 & 031 & 25\\ \hline 0.000 & 5\\ \hline 0.05 & 1\\ \hline 1.12 & 1\\ \hline 0.001 & 102 & 311\\ 1.102 & 311 \end{array}$

Units	Long Tons	Kilograms	Metric Tons
l avoirdupois ounce = l avoirdupois pound = l short hundredweight = l short ton = l long ton = l kilogram = l metric ton =	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		

Units	Grains	Apothecaries Scruples	Pennyweights	Avoirdupois Drams
i grain l apoth. scruple l pennyweight l avdp. dram l apoth. dram l avdp. ounce l apoth. or troy ounce l apoth. or troy pound l avdp. pound l milligram l gram l kilogram	$ \begin{array}{c} = & \frac{1}{20} \\ = & \frac{20}{24} \\ = & \frac{27.343}{75} \\ = & \frac{437.5}{60} \\ = & \frac{437.5}{760} \\ = & \frac{5760}{7000} \\ = & 0.01543236 \\ = & 15.43236 \\ = & 15432.36 \end{array} $	$\begin{array}{c c} \underline{0.05} & \underline{1} \\ \underline{1.2} & \underline{1.367\ 187\ 5} \\ \underline{21.875} & \underline{3} \\ \underline{21.875} & \underline{24} \\ \underline{288} \\ \underline{350} \\ 0.000\ 771\ 617\ 9 \\ 771.617\ 9 \end{array}$	$\begin{array}{c} 0.041 \ 666 \ 67 \\ 0.833 \ 333 \ 3 \\ \hline 1.139 \ 323 \\ \hline 2.5 \\ \hline 18.229 \ 17 \\ \hline 291.666 \ 7 \\ 0.000 \ 643 \ 014 \ 9 \\ \hline 643.014 \ 9 \end{array}$	$\begin{array}{c} 0.\ 036\ 571\ 43\\ 0.\ 731\ 428\ 6\\ 0.\ 877\ 714\ 3\\ \hline 2.\ 194\ 286\ \hline 16\\ 17.\ 554\ 29\ \\ 210.\ 651\ 4\\ 0.\ 000\ 564\ 383\ 4\\ \hline 0.\ 564\ 383\ 4\\ \hline 564\ 383\ 4\\ \end{array}$

## UNITS OF MASS NOT GREATER THAN POUNDS AND KILOGRAMS

Units	Apothecaries Drams	Avoirdupois Ounces	Apothecaries or Troy Ounces	Apothecaries or Troy Pounds
l grain l apoth. scruple l pennyweight l avdp. dram l aydp. dram l avdp. ounce l apoth. or troy ounce l apoth. or troy pound l avdp. pound l milligram l gram l kilogram	$\begin{array}{c} 0.\ 016\ 666\ 67\\ 0.\ 333\ 333\ 3\\ \hline 0.\ 4\\ \hline 0.\ 455\ 729\ 2\\ \hline 7.291\ 667\ \hline \\ \hline 96\\ 116.\ 666\ 7\\ 0.\ 000\ 257\ 206\ 0\\ 0.\ 257\ 206\ 0\\ 257\ 206\ 0\\ \end{array}$	$\begin{array}{c} 0.\ 002\ 285\ 714\\ 0.\ 045\ 714\ 29\\ 0.\ 054\ 857\ 14\\ \underline{0.\ 062\ 5}\\ 0.\ 137\ 142\ 9\\ 1.\ 097\ 143\\ 13.\ 165\ 71\\ 0.\ 000\ 035\ 273\ 96\\ 35.\ 273\ 96\\ \end{array}$	$\begin{array}{c} 0.002 & 083 & 333 \\ 0.041 & 666 & 67 \\ \hline 0.05 \\ \hline 0.056 & 966 & 15 \\ \hline 0.125 \\ \hline 0.911 & 458 & 3 \\ \hline 14.583 & 33 \\ 0.000 & 032 & 150 & 75 \\ 0.032 & 150 & 75 \\ 32.150 & 75 \\ \hline \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

Units	Avoirdupois Pounds	Milligrams	Grams	Kilograms
l grain l apoth. scruple l pennyweight l avdp. dram l apoth. dram l avdp. ounce l apoth. or troy ounce l apoth. or troy pound l avdp. pound l milligram l gram l kilogram	$      0.000 142 857 1 \\      0.002 857 143 \\      0.003 428 571 \\      0.003 906 25 \\      0.008 571 429 \\      0.062 5 \\      0.068 571 43 \\      0.822 857 1 \\      0.000 002 204 623 \\      2.204 623 \\                                  $	$\begin{array}{r} & \begin{array}{r} 64.798 & 91 \\ 1\overline{295.978} & 2 \\ \hline 1555.173 & 84 \\ 1771.845 & 195 & 312 & 5 \\ \hline 387.934 & 6 \\ \hline 28 & 349.523 & 125 \\ \hline 31 & 103.476 & 8 \\ \hline 373 & 241.721 & 6 \\ \hline 453 & 592.37 \\ \hline \\ \hline 1 & 000 & 000 \\ \hline \end{array}$	$\begin{array}{c} \underbrace{\begin{array}{c} 0.064 & 798 & 91 \\ \hline 1.295 & 978 & 2 \\ \hline 1.555 & 173 & 84 \\ \hline 1.771 & 845 & 195 & 312 & 5 \\ \hline 3.887 & 934 & 6 \\ \hline 28.349 & 523 & 125 \\ \hline 31.103 & 476 & 8 \\ \hline 373.241 & 721 & 6 \\ \hline 453.592 & 37 \\ \hline 0.001 \\ \hline 1 & 000 \end{array}$	$ \begin{array}{c} 0.000 & 064 & 798 & 91 \\ 0.001 & 295 & 978 & 2 \\ 0.001 & 555 & 173 & 84 \\ 3.001 & 771 & 845 & 195 & 312 & 5 \\ \hline 0.003 & 887 & 934 & 6 \\ 0.028 & 349 & 523 & 125 \\ \hline 0.031 & 103 & 476 & 8 \\ 0.373 & 241 & 721 & 6 \\ \hline 0.453 & 592 & 37 \\ \hline 0.000 & 001 \\ \hline 0.001 & 1 \\ \hline \end{array} $

## 5.5. Tables of Equivalents

When the name of a unit is enclosed in brackets (thus, [1 hand] . . . ), this indicates (1) that the unit is not in general current use in the United States, or (2) that the unit is believed to be based on "custom and usage" rather than on formal authoritative definition.

Equivalents involving decimals are, in most instances, rounded off to the third decimal place except where they are exact, in which cases these exact equivalents are so designated.

l angstrom (A) <sup>g</sup>	<pre>0.1 millimicron (exactly). 0.000 1 micron (exactly). 0.000 000 1 millimeter (exactly). 0.000 000 004 inch. (120 fathems.</pre>
l cable's length	720 feet. 219.456 meters (exactly).
l centimeter (cm)	0.393 7 inch.
l chain (ch) (Gunter's or surveyors)	(66 feet. 20.1168 meters (exactly).
[1 chain] (engineers)	100  teet.
l decimeter (dm)	-3.937 inches
l dekameter (dkm)	32.808 feet.
l fath and	6 feet.
1 latnom	1.8288 meters (exactly).
l foot (ft)	0.3048 meter (exactly).
	(10 chains (surveyors).
	660 feet.
1 furlong (fur.)	220 yards.
	201 168 motors (ovactly)
[] hand]	4 inches
1 inch (in.)	2.54 centimeters (exactly).
1 kilometer (km)	0.621 mile.
1 log rug (lond)	$\int 3 \text{ statute miles.}$
i league (land)	\4 828 kilometers.
l link (li) (Gunter's or surveyors)	$\begin{cases} 7.92 \text{ inches (exactly).} \\ 0.201 168 \text{ meter (exactly).} \end{cases}$
[1 link (li) (engineers)]	{] foot. 0.3048 meter (exactly).
1 meter (m)	(39.37 inches. (1.094 yards.
l micron (µ[the Greek letter mu])	{0.001 millimeter (exactly). 0.000 039 37 inch.
1 mil	{0.001 inch (exactly). (0.025 4 millimeter (exactly).

## LENGTHS

 $^{g}$ The angstrom is basically defined as  $10^{-10}$  meter.

1	mile (mi) (statute or land)	(5 280 feet. 1.609 kilometers.
1	mile (mi) (nautical, international) <sup>h</sup> -	(1.852 kilometers (exactly). 1.151 statute miles.
1	millimeter (mm)	0.039 37 inch.
1	millimicron (mµ [the English letter m in combination with the Greek letter mu])	$\begin{cases} 0.001 \text{ micron (exactly).} \\ 0.000 000 039 37 \text{ inch.} \end{cases}$
1	point (typography)	0.013 837 inch (exactly). 1/72 inch (approximately). 0.351 millimeter.
1	rod (rd), pole, or perch	$\begin{cases} 16 \ 1/2 \ \text{feet.} \\ 5 \ 1/2 \ \text{yards.} \\ 5.0292 \ \text{meters} \ (\text{exactly}). \end{cases}$
1	yard (yd)	0.9144 meter (exactly).

# AREAS OR SURFACES

	(43 560 square feet.
l acre <sup>1</sup>	4 840 square yards.
	0,405 hectare.
1	119.599 square yards.
1 are	(0.025 acre.
l hectare	2.471 acres.
[1 square (building)]	100 square feet.
l square centimeter (cm <sup>2</sup> )	0.155 square inch.
1 square decimeter (dm <sup>2</sup> )	15.500 square inches.
1 square foot (sq ft)	929.030 square centimeters.
l square inch (sq in.)	6.4516 square centimeters (exactly).
1 aque no bilometer (km <sup>2</sup> )	247.105 acres.
i square knometer (km )	0.386 square mile.
$1 \text{ square meter } (m^2)$	<pre>{1.196 square yards.</pre>
i square meter (m)	\10.764 square feet.
1 square mile (sq mi)	258.999 hectares.
1 square millimeter (mm <sup>2</sup> )	0.002 square inch.
l square rod (sq rd), sq pole, or	
sq perch	25.293 square meters.
1 square yard (sq yd)	0.836 square meter.

<sup>h</sup>The international nautical mile of 1 852 meters (6 076.115 49 . . . feet) was adopted effective July 1, 1954 for use in the United States. The value formerly used in the United States was 6 080.20 feet = 1 nautical (geographical or sea) mile.

<sup>i</sup>The question is often asked as to the length of a side of an acre of ground. An acre is a unit of area containing 43 560 square feet. It is not necessarily square, or even rectangular. But, if it is square then the length of a side is equal to  $\sqrt{43560} = 208.710 + \text{feet}.$ 

## CAPACITIES OR VOLUMES

l barrel (bbl), liquid	31 to 42 gallons. <sup>j</sup>
l barrel (bbl), standard for fruits.	7 056 cubic inches.
vegetables, and other dry com-	105 dry quarts.
modities except cranberries	3.281 bushels, struck measure.
······································	5 826 cubic inches.
l barrel (bbl), standard, cranberry <	86 45/64 dry guarts.
	2.709 bushels, struck measure.
	2 150.42 cubic inches (exactly).
l bushel (bu) (U.S.) struck measure {	35.238 liters.
	2 747.715 cubic inches.
[I bushel, heaped (U.S.)] {	1.278 bushels, struck measure, k
[1 bushel (bu) (British Imperial)	1.032 U.S. bushels, struck measure.
(struck measure)]	2 219. 36 cubic inches.
l cord (cd) (firewood)	128 cubic feet.
l cubic centimeter (cm <sup>3</sup> )	0.061 cubic inch.
l cubic decimeter (dm <sup>3</sup>	61.024 cubic inches.
	7 481 gallons
1 cubic foot (cu ft) {	28 316 cubic decimeters
	0 554 fluid ounce
l cu inch (cu in )	4 433 fluid drams
r cu men (cu me)-	16 387 cubic centimeters.
l cubic meter (m <sup>3</sup> )	1 308 cubic vards.
l cubic yard (cu yd)	0.765 cubic meter
i cubic yara (ca ya)	8 fluid ounces.
l cup, measuring {	1/2 liquid pint.
	1/8 fluid ounce.
	0.226 cubic inch.
l dram, fluid (or liquid) (fl dr or	3.697 milliliters.
f(J) (U.S.)	1.041 British fluid drachms.
	0.961 U.S. fluid dram.
[] drachm, fluid (fl dr) (British)] (	0.217 cubic inch.
	3.552 milliliters.
$\tilde{\mathbf{r}}$	2.642 gallons.
l dekaliter (dkl) {	1.135 pecks.
(	231 cubic inches.
	3.785 liters.
ا gallon (gal) (U. S.) ۲	0.833 British gallon.
	128 U.S. fluid ounces.
	277.42 cubic inches.
	1.201 U.S. gallons.
[I gallon (gal) (British Imperial)] {	4.546 liters.
	160 British fluid ounces.
	7.219 cubic inches.
1 gill (gi) <	4 fluid ounces.
	0.118 liter.
	26.418 gallons.
1 nectoliter (hl) {	2.838 bushels.
(	~

<sup>j</sup>There are a variety of "barrels" established by law or usage. For example, Federal taxes on fermented liquors are based on a barrel of 31 gallons; many State laws fix the "barrel for liquids" as 31 1/2 gallons; one State fixes a 36-gallon barrel for cistern measurement; Federal law recognizes a 40-gallon barrel for "proof spirits"; by custom, 42 gallons comprise a barrel of crude oil or petroleum products for statistical purposes, and this equivalent is recognized "for liquids" by four States.

<sup>k</sup>Frequently recognized as 1 1/4 bushels, struck measure.

	(1.057 liquid quarts.
1 liter	0.908 dry quart.
	61.025 cubic inches.
	0.271 fluid dram.
1 milliliter (ml)	(16.231 minims.
/	0.061 cubic inch.
lounce, fluid (or liquid) (fl oz or	1.805 cubic inches.
f = (U, S, )	29.573 milliliters.
	1.041 British fluid ounces.
	J0.961 U. S. fluid ounce.
[1 ounce, fluid (fl oz) (British)]	1.734 cubic inches.
	28.412 milliliters.
1 peck (pk)	8.810 liters.
	/33.600 cubic inches.
1 pint (pt), dry	0.551 liter.
1 wint (wh) liquid	$\int 28.875$ cubic inches (exactly).
1 pint (pt), 11quia	0.473 liter.
	(67.201 cubic inches.
l quart (qt), dry (U. S.)	(1.101 liters.
	0.969 British quart.
	(57.75 cubic inches (exactly).
l quart (qt), liquid (U. S.)	0.946 liter.
	(0.833 British quart.
	(69.354 cubic inches.
[1 quart (qt) (British)]	1.032 U. S. dry quarts.
	(1.201 U. S. liquid quarts.
	3 teaspoons. <sup>1</sup>
l tablespoon	4 fluid drams.
	1/2 fluid ounce.
l teaspoon	1/3 tablespoon. <sup>1</sup>
	(1 1/3 fluid drams. <sup>1</sup>
1 water ton (English)	[270.91 U. S. gallons.
	(224 British Imperial gallons (exactly).

## WEIGHTS OR MASSES

1	assay ton <sup>m</sup> (AT)	29.167 grams.
1	carat (c)	∫200 milligrams.
1		3.086 grains.
1	dram, apothecaries (dr ap or $f$ 3)	60 grains.
1	dram, avoirdupois (dr avdp)	$(27 \ 11/32 \ (= 27.344) \text{ grains}.$
	gamma, <u>see</u> microgram.	(1.772 grams.

<sup>1</sup>The equivalent "1 teaspoon=1 1/3 fluid drams" has been found by the Bureau to correspond more closely with the actual capacities of "measuring" and silver teaspoons than the equivalent "1 teaspoon=1 fluid dram," which is given by a number of dictionaries.

<sup>m</sup>Used in assaying. The assay ton bears the same relation to the milligram that a ton of 2 000 pounds avoirdupois bears to the ounce troy; hence the weight in milligrams of precious metal obrained from one assay ton of ore gives directly the number of troy ounces to the net ton.

<sup>n</sup>The gross or long ton and hundredweight are used commercially in the United States to only a very limited extent, usually in restricted industrial fields. These units are the same as the British "ton" and "hundredweight."

<sup>o</sup>The symbol  $\gamma$  [the Greek letter gamma] is also used.

<sup>P</sup>The gross or long ton and hundredweight are used commercially in the United States to a limited extent only, usually in restricted industrial fields. These units are the same as the British "ton" and "hundredweight."

Prepared by: Lewis V. Judson Office of Weights and Measures National Bureau of Standards

# REDEFINITION OF THE METER

In October 1960, the Eleventh General (International) Conference on Weights and Measures redefined the meter as 1 650 763.73 wavelengths of the orange-red radiation in vacuum of krypton 86 corresponding to the unperturbed transition between the  $2p_{10}$  and 5d5 levels. The platinum-iridium meter bars will remain important because of the ease with which they can be used for certain types of measurements. (See pages 5, 6, 9, and 10.)

Paragraph added November 1960.

#### \* \* \* \* \* \*

## NEW STANDARDS OF LENGTH, MASS, AND TIME

There is considerable interest manifested at this time in proposed new standards of length, mass, and time, based on constants of nature.

A new standard of length has already been adopted. See paragraph above.

Although proposals have been made of possible atomic standards of mass, it is unlikely that the unit of mass, the kilogram, will be more accurately defined in the near future. There does not seem to be any strong reason for replacing the present prototype with a physical constant.

In the measurement of time a further development beyond the present definition of the second has been suggested. We can now measure the resonance frequencies associated with various atomic transitions with greater precision than we can measure the second as it is now defined. The fact seems to be that a physical constant, the frequency associated with a particular transition of the cesium atom, would be a better standard for time-intervals and frequency than an astronomical constant and, furthermore, a standard of this nature would be more readily accessible to working laboratories. Other atomic frequencies are also being studied, and it may be expected that in the next few years international accord will be reached on a new definition of the second based upon an atomic constant.

Paragraph added October 20, 1961